

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet: Linearna algebra in optimizacija
Course title: Linear Algebra and Optimization

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Podatkovne znanosti, magistrski študijski program druge stopnje	-	Prvi	Prvi
The second cycle master's study programme Data Sciences	-	First	First

Vrsta predmeta / Course type

Obvezni/ Obligatory

Univerzitetna koda predmeta / University course code:

2-PZ-MAG-LAO-2026-09-29

Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS
30	-	25	-	10	115	6

Nosilec predmeta / Lecturer: Izr. prof. dr. Vesna Andova

Jeziki / Languages:

Predavanja / Lectures: Slovenski / Slovenian, Angleški / English
Vaje / Tutorial: Slovenski / Slovenian, Angleški / English

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Specifičnih pogojev za vključitev v delo ni.

Priporočeno je poznavanje osnovnih matematičnih pojmov in računanja z matrikami.

Pogoj za pristop k pisnemu izpitu je pravočasna oddaja in pozitivna ocena domačih nalog.

Prerequisites:

There are no specific requirements for this subject.

Knowledge of basic mathematical notions and matrix computations is recommended.

Student has to submit homework assignments within the due time. If the assignments are positively graded, he/she is allowed to write the exam.

Vsebina:

- Ponovitev osnovnih pojmov linearne algebre (matrike in determinante).
- Vektorji.
- Vektorski prostori.
- Linearna odvisnost in neodvisnost.

Content (Syllabus outline):

- Repetition of basic concepts of linear algebra (matrices and determinants).
- Vectors.
- Vector spaces.

- Baze in dimenzije.
- Linearne kombinacije in razponi.
- Inverz matrik.
- Rang matrik.
- Lastne vrednosti in lastni vektorji.
- Linearne transformacije.
- Norme, notranji produkti in ortogonalnost.
- Matrične dekompozicije.
- Psevdo inverz.
- Računanje z velikimi matrikami.
- Konveksnost in Newtonova metoda.
- Lagrangevi multiplikatorji.

- Linear dependence and independence.
- Basis and dimension.
- Linear combinations and spans.
- Matrix inversion.
- Rank.
- Eigenvalues and eigenvectors.
- Linear transformations.
- Norms, inner products and orthogonality.
- Matrix decomposition.
- Pseudoinverse.
- Computations with large matrices.
- Convexity and Newton's method.
- Lagrange multipliers.

Temeljni literatura in viri / Readings:

- B. Magajna, Linearna algebra, metrični prostor in funkcije več spremenljivk, DMFA-založništvo, 2011.
- I. Vidav, Algebra, DMFA-založništvo, 2003.
- P. Lancaster, M. Tismenetsky, The Theory of Matrices, Academic Press, 2007.
- G. Strang, Introduction to Linear algebra, Wellesley-Cambridge Press, 2016.
- G. Strang, Linear Algebra and Learning from Data, Wellesley-Cambridge Press, 2019.
- S. Axler, Linear Algebra Done Right, Springer, 1997.

Cilji in kompetence:

Učna enota prispeva k razvoju naslednjih splošnih in predmetno-specifičnih kompetenc:

Splošne kompetence:

- Sposobnost analitičnega in algoritmičnega razmišljanja.
- Sposobnost fleksibilne uporabe znanja v praksi.

Predmetno-specifične kompetence:

- Sposobnost reševanja problemov z uporabo linearne algebre.
- Razumevanje logičnih dokazov in aksiomatskih metod, ki se uporabljajo v linearni algebri.
- Sposobnost povezovanja linearne algebre z drugimi področji.
- Poznavanje programskega jezika Matlab, R ali Python.

Objectives and competences:

The instructional unit contributes to the development of the following general and subject-specific competences:

General competencies:

- The ability of analytical and algorithmic thinking.
- The ability of flexible usage of knowledge in practice.

Subject-specific competencies:

- Ability to solve problems using linear algebra.
- Understanding logical proofs and the axiomatic method as applied to linear algebra.
- Ability to connect linear algebra to other fields both within and without mathematics.
- Ability to use programming language Matlab, R or Python.

Predvideni študijski rezultati:

Znanje in razumevanje:

- Študentje bodo spoznali zahtevnejše pojme in principe linearne algebre.
- Študentje bodo sposobni prepoznati praktične probleme in jih reševati z orodji linearne algebre.
- Poznali in razumeli bodo pglavitne izreke linearne algebre.
- Spoznali bodo metode matematične optimizacije.
- Spoznali se bodo s programskih jezikom Matlab, R ali Python.

Prenosljive spretnosti:

- Pridobljeno znanje bo prenosljivo na druga področja, predvsem na področji statistike in strojnega učenja.

Intended learning outcomes:

Knowledge and understanding:

- Students will get acquainted with advanced notions and principles of linear algebra.
- Students will be able to recognize practical problems and solve them with linear algebra tools.
- They will know and understand fundamental theorems of linear algebra.
- They will learn methods from mathematical optimization.
- They will learn to use programming languages Matlab, R or Python.

Transferable skills:

- Acquired knowledge will be transferable to other areas, mainly to statistics and machine learning.

Metode poučevanja in učenja:

- Predavanja z aktivno udeležbo študentov (razlaga, diskusija, vprašanja, primeri).
- Vaje (reševanje problemov).
- Učenje na osnovi problemov.
- Samostojno študiranje pod nadzorom (dodelitev teme, ki jih študenti raziskujejo pod nadzorom, pri čemer se nudi povratne informacije in usmerjanje).

Learning and teaching methods:

- Lectures with active students' participation (explanations, discussion, questions, examples)
- Exercises (problem solving).
- Problem-based learning.
- Supervised independent study (assign topics for students to explore under supervision, providing feedback and guidance).

Načini ocenjevanja:

Delež (v %) /

Weight (in %)

Assessment:

• Pisni izpit	100 %	• Written exam
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Reference nosilca / Lecturer's references:

- V. Andova, M. Knor, R. Škrekovski, Distances based indices on nanotubical graphs: part 2, J. Math. Chem. 56 (2018) 3076-3088.
- V. Andova, M. Knor, R. Škrekovski, Distances based indices on nanotubical graphs: part 1, J. Math. Chem. 56 (2018) 2801-2815.
- V. Andova, B. Lidický, B. Lužar, R. Škrekovski, On facial unique-maximum (edge)coloring, Discrete Applied Math. 237 (2018) 26-32.
- V. Andova, S. Atanasova, E. Jovcevska, V. Jordanova, I. Tolovski, M. Rizov, Projecting a hydrographic map of Republic of Macedonia, J. Electrical Engineering and Information Technologies, 1-2 (2016) 93-100.

- V. Andova, D. Orlić, R. Škrekovski, Leapfrog fullerenes and Wiener index, *Applied Math. Comp.* 309 (2017) 281-288.
- V. Andova, M. Knor, R. Škrekovski, Distances on nanotubical graphs, *J.Math. Chem.* 54(8) (2016) 1575-1584.
- V. Andova, F. Kardoš, R. Škrekovski, Mathematical aspect on fullerenes, *Ars Mathematica Contemporanea*, 11 (2016) 353-379.
- V. Andova, D. Blenkuš, T. Došlić, F. Kardoš, R. Škrekovski, On diameter of nanotubical fullerene graphs, *MATCH Commun. Math. Comput. Chem.* 73 (2015) 529-542.
- V. Andova, F. Kardoš, R. Škrekovski, Sandwiching saturation number of fullerene graph, *MATCH Commun. Math. Comput. Chem.* 73 (2015) 501-517.
- Y. Alizadeh, V. Andova, S. Klavžar, R. Škrekovski, Wiener Dimension: Fundamental Properties and (5,0)-Nanotubical Fullerenes, *MATCH Commun. Math. Comput. Chem.* 72 (2014) 279-294.